

Software Engineering

(6) Testing

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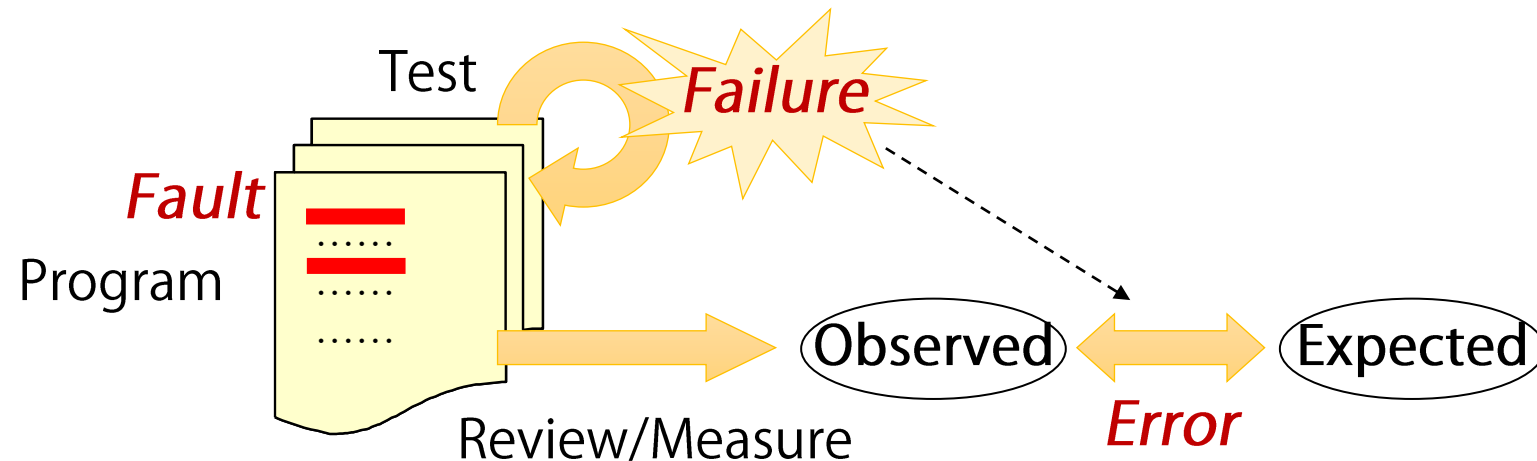
- Overview
- Overview of Each Test Phase
- Whitebox Testing
- Blackbox Testing
- Combinational Testing

Testing

■ Testing

Analyze the target software and try to cause failures for detecting bugs (defects, faults)

- The most practical way for V&V on the program code
- Cannot ensure to detect all the bugs



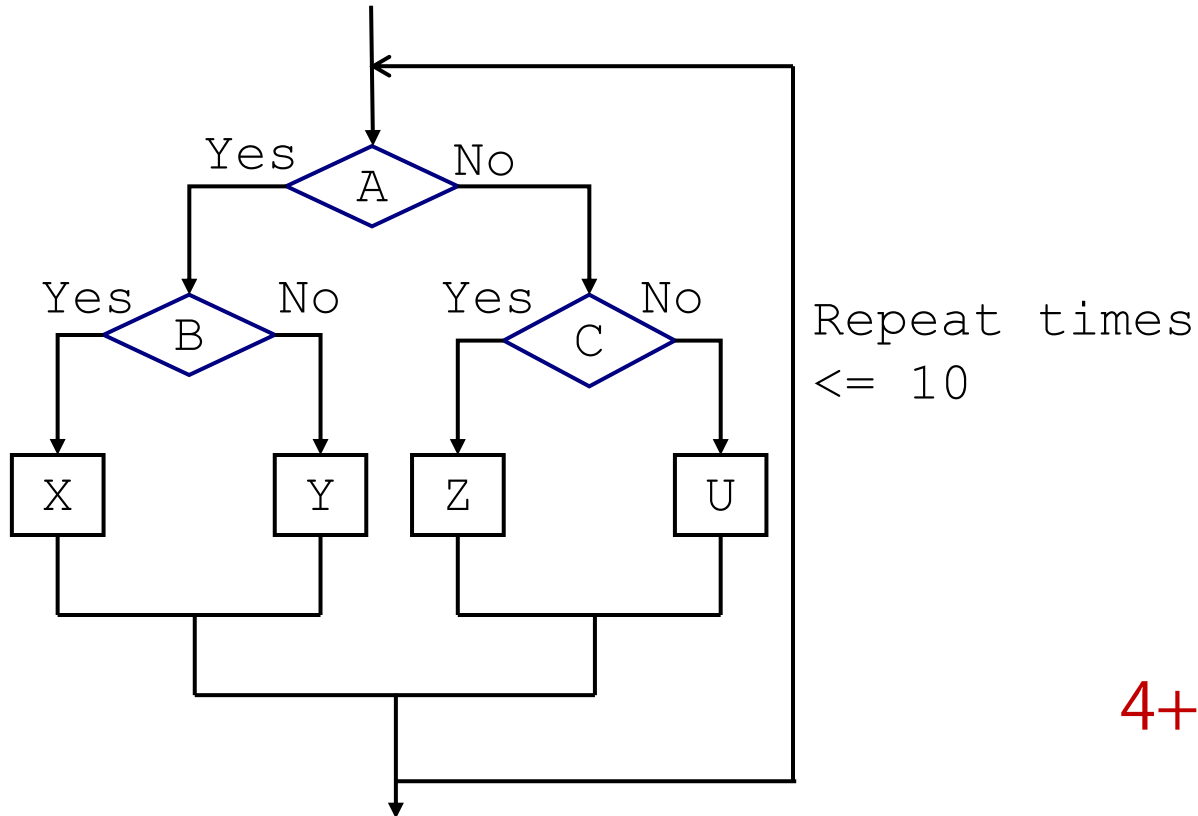
Terminology

- **Error (エラー)** : difference between the theoretical correct value/condition and the computed/observed/measured one
- **Fault (障害, バグ, 不具合)** : wrong steps, process, or data definition in the program code
- **Failure (故障)** : state in which required functions are not provided

*Different terminologies/translations exist,
e.g., "fault" in "fault-tolerance" is translated as 「故障」*

Question: what are “good” tests?

- Example: how many executions required to try all the possible execution paths?



$$4 + 4^2 + 4^3 + \dots + 4^{10} \geq 10^6$$

Question: what are “good” tests?

- Achieve the “best” with the minimum effort, assuming we cannot be perfect
 - Example: compare two **test suites** for a program expected to calculate the absolute value of the input

```
if (x>=1) return x else return -x
```

Test suite 1

1. input x = 3, check the result is 3
2. input x = 5, check the result is 5

Test suite 2

1. input x = 3, check the result is 3
2. input x = -3, check the result is 3

Myers Triangle Problem

- Define a test suite for the following target problem
 - Reads three integer values from the console
 - Outputs a type of triangles with the side lengths of the values: “regular triangle,” “isosceles triangle,” or “scalene triangle”

Myers Triangle Problem: checklist (1)

1. Included a case for a valid scalene triangle?
2. Included a case for a valid regular triangle?
3. Included a case for a valid isosceles triangle?
4. In #3, included at least three cases with different orders (regarding the position of the two same values)?
e.g., (3, 3, 4) (3, 4, 3) (4, 3, 3)
5. Included a case in which one of the value is 0?
6. Included a case in which one of the value is negative?

Myers Triangle Problem: checklist (2)

7. Included a case in which one of the values equals to the sum of the other two values?
e.g., (1, 2, 3)
8. In #7, included at least three cases with different orders?
(regarding the position of)
e.g., (1, 2, 3), (1, 3, 2), (3, 1, 2)
9. Included a case in which one of the values is more than the sum of the other two values?
10. In #9, included at least three cases with different orders?

Myers Triangle Problem: checklist (3)

11. Included the case with all the values as 0?
12. Included a case with a non-integer value?
13. Included a case with a wrong number of inputs?
14. Defined the expected outputs for all of the test cases?

Myers Triangle Problem: Summary

- Each of the different test cases (except for the last item) correspond to different types of possible faults
 - 7.8/14
(Probably improved now?)
- ➔ Need systematic principles/methods to derive such test cases

Other Topics in Testing (1) Termination Criteria

■ Naive termination criteria

- “When we ran out the time/budget”: easy but not essential
- “When we didn’t find any bug”: may lead to “weak” tests with less bug-finding capability

■ Statistics and heuristics

- e.g., comparison with known average values for detected bugs for the size of the target program
- e.g., convergence in the number of detected bugs in a certain time period

Other Topics in Testing (2) Mental Aspects

- Principles based on the mental aspects
 - Define the expected outputs beforehand
 - Not test the program of your own
 - Make test cases for wrong inputs
 - Investigate also there is no unintended behavior
 - Not expect “there should not be any error”
 - Expect more errors in the part where many errors were found
 - Not criticize the coder
 - Think testing as creative challenges

Classification (1) Whitebox/Blackbox

■ Whitebox testing

- Design tests by considering the internal structure of the program code
 - e.g., make tests for both of the branches in an if-else statement

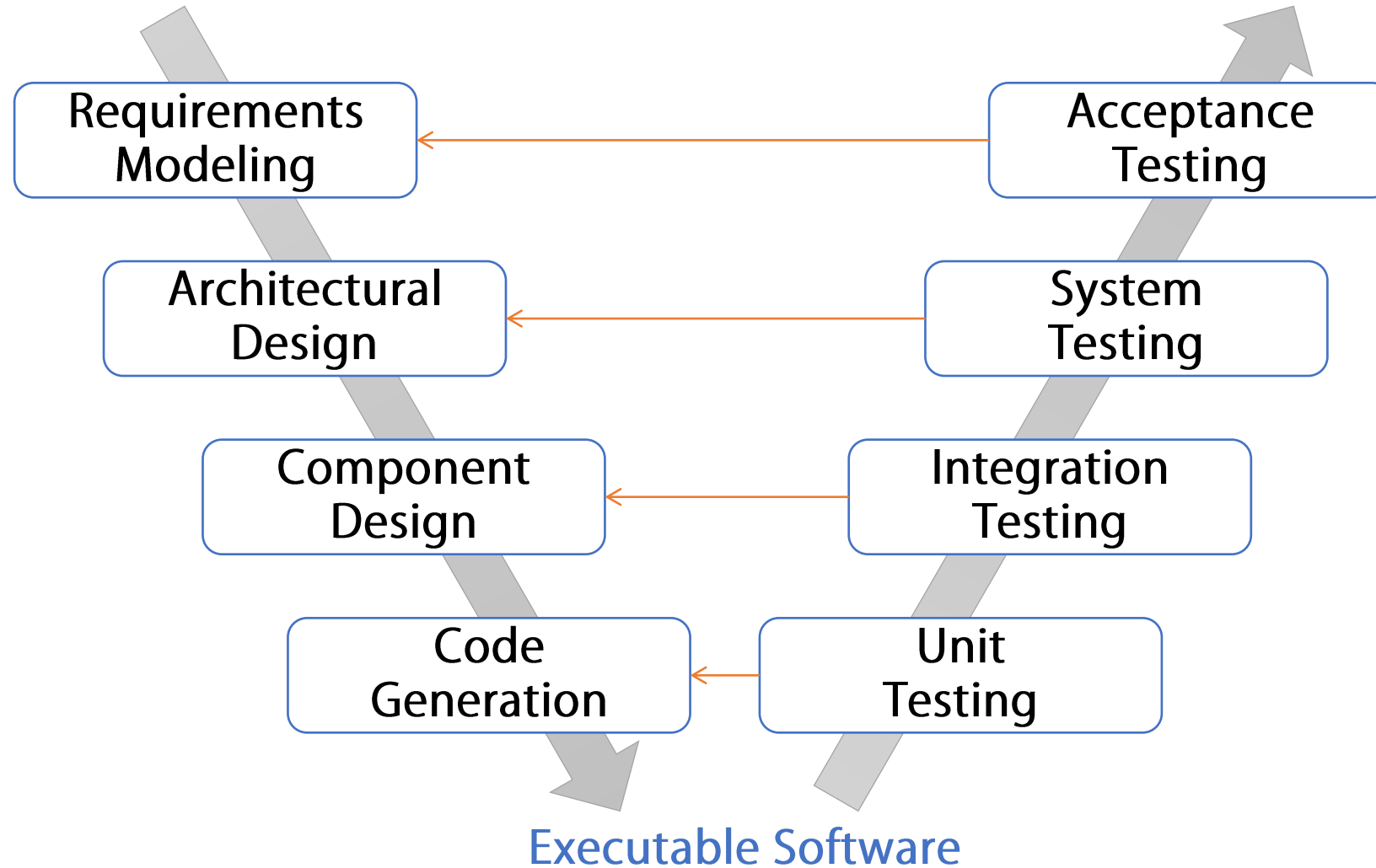
■ Blackbox testing

- Design tests only by considering the specification
 - e.g., make tests based on use cases

Classification (2) Phases

- **Unit Testing** (ユニットテスト・単体テスト)
 - Target small components such as methods
- **Integration Testing** (結合テスト・統合テスト)
 - Target combination of (already tested) components
- **System Testing** (システムテスト)
 - Target system elements such as network, hardware, and database
- **Acceptance Testing** (受け入れテスト)
 - Target actual operation including user satisfaction, load, long-term operation

(Review) The V Process Model



[C. Bucanac, 1999]

Regression Testing

■ Regression Testing (回帰テスト)

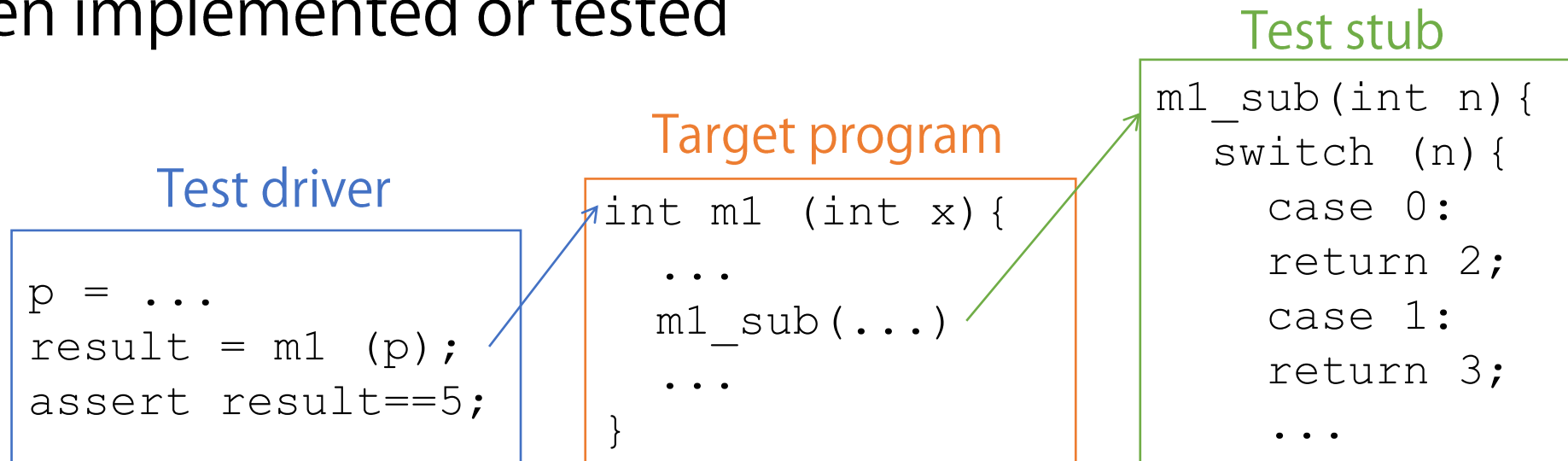
- Check whether something is worse than the previous version
- Background: it is very typical that a fix for a certain function leads to failures in other parts
(Japanese engineers often say 「デグレ」 for degradation)

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Basic Concept: Test Driver and Stub

- We want to focus on **SUT (System Under Test)** in each test by excluding possibilities of bugs in other parts
 - **Test driver**: invoke the SUT and observe the outcome
 - **Test stub**: provide pseudo functions for components that have not been implemented or tested



Unit Testing

- Focus on specific small components by making use of test drivers and stubs
- Often use popular XUnit frameworks
 - Junit, CppUnit, PHPUnit, unittest (Python), ...
 - Define each test case separately, and execute them again and again

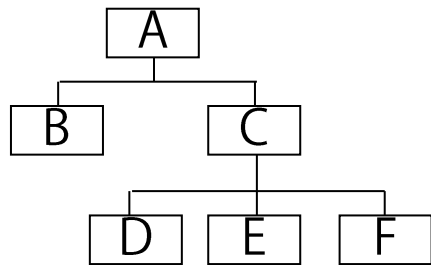
```
public class TestCase1
    extends TestCase{
    public void testFun1(){
        ...
        assertEquals( x, 3 );
    }
}
```

```
suite.addTest(new TestCase1());
suite.addTest(new TestCase2());
...
suite.run(result);
...
```

*(now tools automatically
collects defined tests in
a project)*

Integration Testing

- Gradually integrate and test combinations of components
 - Otherwise, it's hard to identify the bug (big-bang)
 - **Incremental Testing**
 - Top-down vs. bottom-up: bottom-up is easier to do in parallel with coding but may encounter large rollbacks as the key function at the top level is tested last



Top-down

1. A and B
(with C stub)
2. A, B, and C
(with D, E, F stubs)
3. A, B, C, and D
(with E, F stubs)
4. ...

Bottom-up

1. C and D
(with E, F stubs)
2. C, D, and E
(with F stub)
3. C, D, E, and F
4. ...

System Testing and Acceptance Testing

- Various system-level aspects
 - Stress, performance, volume, usability, security, compatibility, portability, document-understandability, ...
- Acceptance testing uses actual users or data

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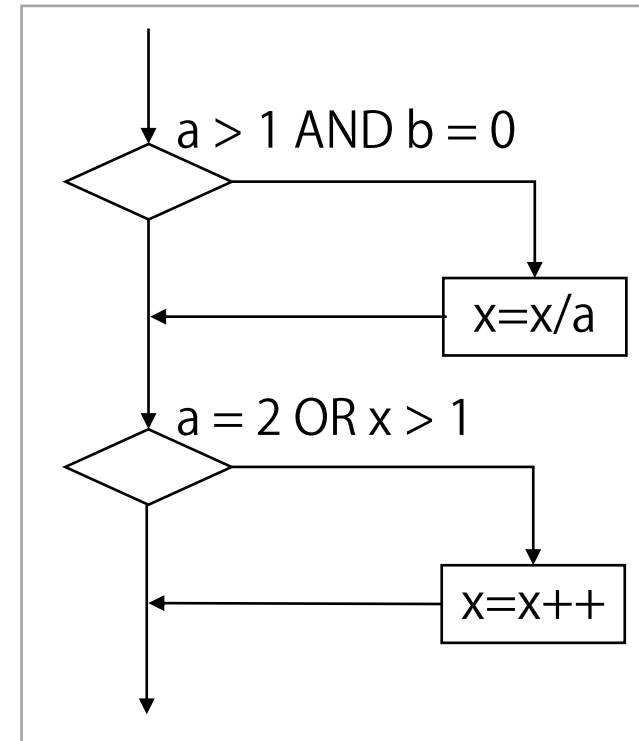
Coverage

- Coverage (カバレッジ, 被覆率) :
how many “elements” were covered by tests?
- Example: if (P and Q) then ... else ...
 - Cover branches (then, else)
→ (P, Q) = (true, true), (false, true) covers 2/2
 - Cover conditions of P and Q (true, false)
→ (P, Q) = (true, true), (false, false) covers 4/4

Statement Coverage

- Statement Coverage (命令網羅, C0)
 - Each statement was executed at least once

e.g., input (a, b, x) = (2, 0, 3)



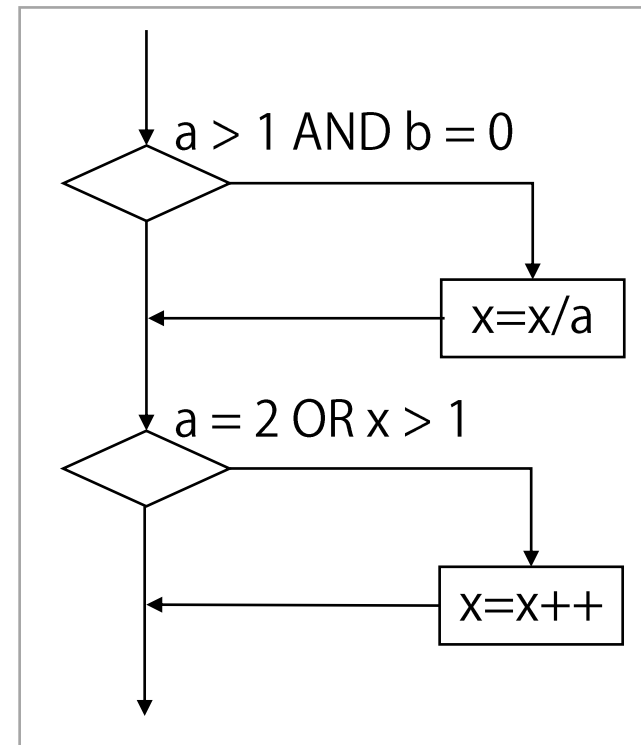
Branch Coverage

■ Branch Coverage / Decision Coverage

(分岐網羅・判定条件網羅, C1)

■ Each statement was executed at least once

e.g., input $(a, b, x) = (3, 0, 3), (2, 1, 1)$



Note on Statement Coverage and Branch Coverage

- We often think branch coverage subsumes statement coverage
- Strictly speaking, there are some situations where a test suite satisfy the branch coverage but not the statement one
 - If there is an unreachable part of the code (this is considered as a bug or undesirable)
 - If there are many entries for the program

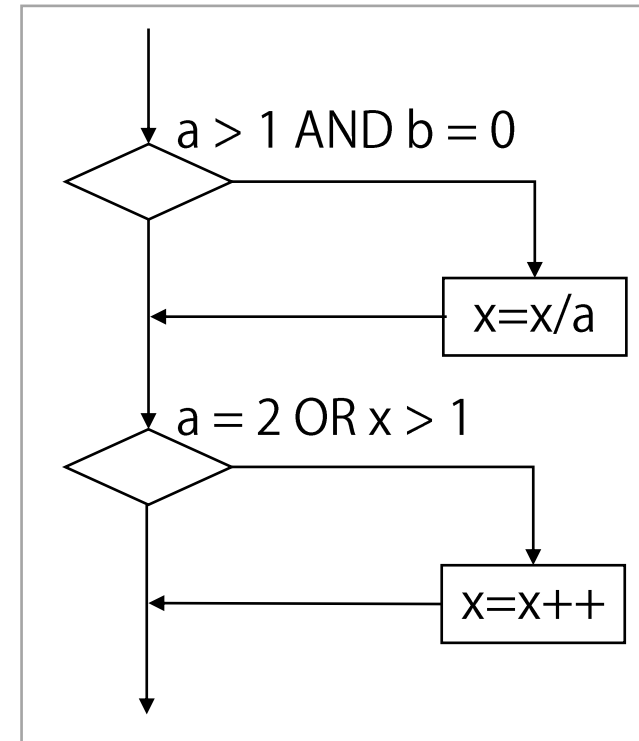
Condition Coverage

■ Condition Coverage (条件網羅, C2)

- Each possible outcome of individual conditions was exposed at least once

e.g., input

$(a, b, x) = (1, 0, 3), (2, 1, 1)$



Note on Branch Coverage and Condition Coverage

- There are some situations where a test suite satisfy the condition coverage but not the branch one
 - e.g., for “if P AND Q”
 $(P, Q) = (\text{true}, \text{false}), (\text{false}, \text{true})$

Multiple-condition Coverage

■ Multiple-condition Coverage (複数条件網羅)

- Each possible combination of possible outcomes in each branch was exposed at least once

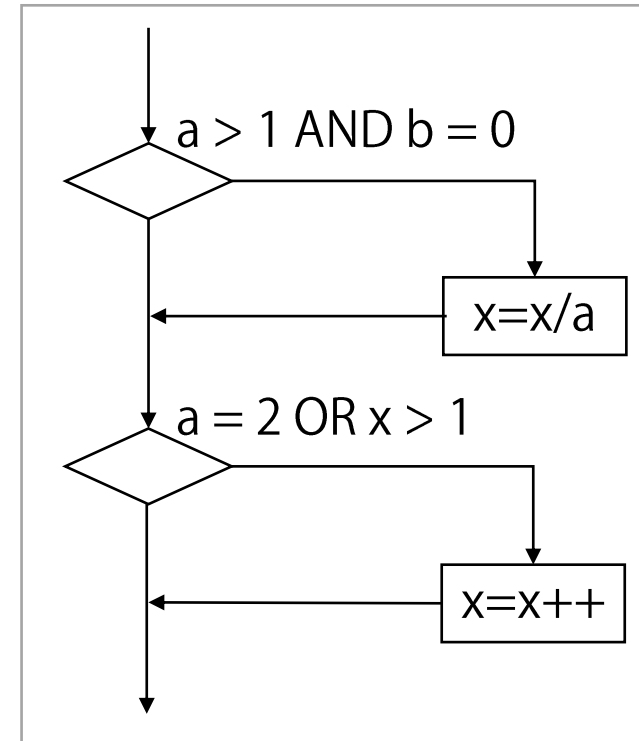
e.g., $(a, b, x) =$

$(2, 0, 4) \rightarrow (T-T, T-T)$

$(2, 1, 1) \rightarrow (T-F, T-F)$

$(1, 0, 2) \rightarrow (F-T, F-T)$

$(1, 1, 1) \rightarrow (F-F, F-F)$



MC/DC

- **MC/DC (Modified Condition/Decision Coverage)**
 - Branch coverage
 - Condition coverage, but “condition covered” means “each condition solely affects the branch decision”
 - ➔ i.e., we don’t think “unused condition value” as “covered”

Example: if (P and Q) then ... else ...

→ (P, Q) = (true, true), (false, false) → 4/4 condition values covered?

→ Q=false was not actually used!

→ We should have (P, Q) = (true, true), (true, false), (false, true)

Practices of Coverage

- 100% is often difficult
 - There may be impossible combinations of condition values
 - It is very difficult to derive a test suite
 - ➔ Thresholds are often defined in each company, e.g., 85%
- Complex coverage criteria are more difficult to achieve and costly to evaluate
 - Branch coverage (C1) is a modest standard?
- Safety-aware domains require MC/DC such as avionics

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Equivalence Partitioning

■ Equivalence Partitioning (同値分割) :

Make classes (groups) of inputs that lead to specific types of behaviors

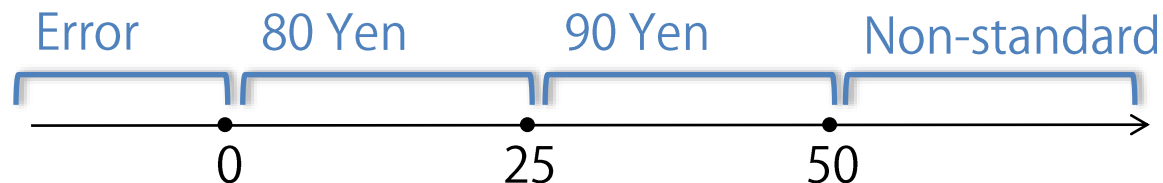
- We should have at least one test case for each equivalent class
- Example: price calculation for standard mail

Weight	Price
$\leq 25\text{g}$	80 Yen
$\leq 50\text{g}$	90 Yen



Necessary test cases (example)

-5g, 10g, 35g, 80g



Equivalence Partitioning: Guidelines

- Guidelines for partitioning
 - An input has range of values or ranges for num. of values
 - ➔ Class for effective inputs, one for too small, one for too large
 - An input has enumeration of possible values
 - ➔ Classes for each value, one for invalid value
 - An input has a condition to satisfy
 - ➔ Class for valid inputs, one for invalid inputs

Equivalence Partitioning: Example

- Example: compiler function to handle array declaration part
 - Num of arrays: 1, 1+, none
 - Length of array name: valid, 0, too long
 - Array name: alphabets, with numbers, with other characters
 - Array dimension: valid, 0, too many
 - Num. of elements in each dimension
 - valid, negative, too many
 - specified, not specified
 - specified as const, specified with int variable, ...

Boundary Value Analysis

- Boundary Value Analysis (境界値分析)
 - Use boundary values in equivalence classes
 - Example: price calculation for standard mail

Weight	Price
$\leq 25\text{g}$	80 Yen
$\leq 50\text{g}$	90 Yen



Necessary test cases

0g, 1g, 25g, 26g, 50g, 51g

Boundary Value Analysis

- Example: sort and print of exam. results
 - Num. of questions: 0, 1, upper-bound, upper-bound+1
 - Num. of students: 0, 1, upper-bound, upper-bound+1
 - Sorting results: all the same, all different
 - Deviation scores: “one score 0 and the others 100”
(max. deviation),
“all the same scores” (deviation 0)
 - Num. of pages: 0, 1, upper-bound, upper-bound+1
 - ...

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Combinational Testing

- Some bugs lead to observable failures only for a certain combinations of multiple factors
 - Web application: OS type/version, browser type/version, browser plug-in version, ...
- There is a logical reason why the specific combination does not work but it is very hard to know that before we actually encounter and investigate the failure
 - i.e., we cannot say “we don’t need tests for this combination”

Combinational Testing

In general,

- When we have n aspects (**factors, 因子**) and each can take a possible values (**levels, 水準**)
 - We have a^n combinations
 - 4 factor, 3 levels for each factor: 81 combinations
 - 10 factor, 3 levels for each factor: 59049 combinations
- ➔ How can we get effective tests with a smaller number of combinations?

Pair Construction

- One idea:

test all the pairs of values from two factors

- Just a heuristic, not without any theoretical guarantee

- Past statistics showed more than half (sometimes 80%) faults could be detected with this strategy

(faults with one aspect and faults with two aspects are dominant)

Pair Construction

■ Example

- Factor: A, B, C
- Level for each factor: 0, 1
- For each of (A, B), (B, C), and (C, A), we cover (0, 0), (0, 1), (1, 0), (1, 1)

	A	B	C
Test case 1	0	0	0
Test case 2	0	1	1
Test case 3	1	0	1
Test case 4	1	1	0

Construction of Test Suite

- Approach 1: prepare tables like the previous one and apply them to the give problem <http://neilsloane.com/oadir/>
- ➔ **Orthogonal Arrays (直交表)**
 - For each column pair (factor pair), all the pairs appear the same number of times
- Approach 2: make an algorithm to generate test suites
 - Exhaustive search does not scale
 - Typically use heuristics or meta-heuristics

Orthogonal Arrays: Parameters

■ Parameters of orthogonal arrays

- The num. of factors c (appears as columns)
- The num. of levels: n
- The num of test cases (appears as rows)

Notation
 $L_x(n^c)$

000
011
101
110

$L_4(2^3)$

0000
0111
0222
1012
1120
1201
2021
2102
2210

$L_9(3^4)$

Orthogonal Arrays: Examples

0000000
1111110
2222220
0012120
1120200
2201010
0102211
1210021
2021101
0220111
1001221
2112001
0121022
1202102
2010212
0211202
1022012
2100122

$L_{18}(3^7)$

0	0	0	0	0
1	1	1	1	0
0	0	1	1	1
1	1	0	0	1
0	1	0	1	2
1	0	1	0	2
0	1	1	0	3
1	0	0	1	3

$L_8(2^4 4^1)$

0000
0011
0101
0110
1001
1010
1100
1111

Cover triples
such as (0, 0, 0), (1, 0, 1)

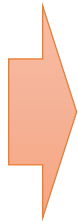
Orthogonal Arrays: Application

■ Application example

■ A: {IE,FF,CH}, B: {ON, OFF}, C: {win,mac,lin}

0000
0111
0222
1012
1120
1201
2021
2102
2210

$L_9(3^4)$



000
011
022
101
112
120
202
210
221



IE	ON	win
IE	OFF	mac
IE	?	lin
FF	ON	mac
FF	OFF	lin
FF	?	win
CH	ON	lin
CH	OFF	win
CH	?	mac



IE	ON	win
IE	OFF	mac
IE	ON	lin
FF	ON	mac
FF	OFF	lin
FF	OFF	win
CH	ON	lin
CH	OFF	win
CH	ON	mac

Remove the 4th column unnecessary

Replace with actual levels

Fill unused levels with arbitrary values

Orthogonal Arrays: Characteristics

- Basically, we cannot remove rows when we customize
 - Probably violating the “all the pairs” constraint
 - Difficult to handle exception or inhibition, i.e., we want to exclude a certain combination
 - What if we cannot include “IE-mac” in the previous example
- All the pairs appear the same number of times
 - Not the minimum to cover all the pairs
 - But covers many triples, quadruples, \dots thanks to the symmetry

All-Pair Method

■ All-Pair method

- Finds a combination by an algorithm to cover all the pairs
- Example for A: {0, 1}, B: {0, 1}, C: {0, 1, 2}

A	B	C
0	0	0
0	1	1
1	0	1
1	1	0
0	0	2
1	1	2



We don't have
0 1 2
1 0 2
compared with
orthogonal array

All-Pair Method: Characteristics

- By good algorithms
 - Much less test cases than orthogonal arrays with symmetry
 - Example: for 100 factors and 2 levels, 101 test cases by orthogonal arrays but 10 by an all-pair algorithm
 - Allows for customization such as inhibition
 - Various approaches
 - Greedy search by generating rows one by one
 - Meta-heuristics such as genetic algorithms
 - Update on existing tables
 - ...

Example of Tool

- PICT

- <https://github.com/Microsoft/pict/blob/main/doc/pict.md>

Logical Combination

- Combinational Testing: without assumptions on logical dependencies between factors
 - No over-confidence on “
- If the logical relationship is clear, we can just organize it to design the tests
 - Decision tables
 - Cause effect graphs

	Rule 1	Rule 2	Rule 3	Rule 4
Condition				
Married	Y	Y	N	N
Student	Y	N	Y	N
Action				
Discount	60	26	50	0

Summary

■ Testing

- Core of V&V activities
- Cannot be perfect and explore the cost-effectiveness by trying to efficiently expose hidden defects
- Employs different approaches for different phases and objectives