# A Semantics of Argumentation under Incomplete Information

Ken Satoh<sup>1</sup>, Kazuko Takahashi<sup>2</sup>

 <sup>1</sup> National Institute of Informatics and Sokendai ksatoh@nii.ac.jp
 <sup>2</sup> School of Science&Technology, Kwansei Gakuin University ktaka@cs.kwansei.ac.jp

**Abstract.** We discuss a semantics of argumentation under incomplete information. In this paper, we mean by "incomplete information" that an agent does not know the other agent's knowledge and therefore, the agent cannot predict which arguments are attacked and which counterarguments are used in order to attack the arguments. In this paper, we provide a more general framework for such argumentation system than previous proposed framework and provide a computational method how to decide acceptability of argument by logic programming if both agents are eager to give all the arguments.

## 1 Introduction

Argumentation system is a hot topic in legal reasoning and in more general setting such as negotiation in multi-agent systems[Rahwan09]. However, most of the work on argumentation is based on the assumption where complete information about argumentation is provided[Dung95]. It would be appropriate for an application domain where we can see all the arguments and counter-arguments so that we can conclude the most appropriate result based on all the arguments. However, in reality, there would be another type of argumentation where relevant agents only have their own belief and they do not know other agents' belief and so they do not predict how other agents attack their own arguments.

Consider the following slightly modified example taken from [Okuno09]<sup>3</sup>.

- p0: "You killed the victim."
- c1: "I did not commit murder! There is no evidence!"
- p1: "There is evidence. We found your ID card near the scene."
- c2: "It's not evidence! I had my ID card stolen!"
- p2: "It is you who killed the victim. Only you were near the scene at the time of the murder."
- c3: "I didn't go there. I was at facility A at that time."
- p3: "At facility A? Then, it's impossible to have had your ID card stolen since facility A does not allow a person to enter without an ID card."

 $<sup>^3</sup>$  In the example, c and p are two parties and numbers attached with c and p express order of arguments.

This kind of argumentation would occur in examinations of witness in legal courts. In the above example, c2 is not firstly attacked but after the argument of c3 is given, c2 is attacked by p3. Since agent p does not believe that the suspect was at facility A, p could not use the counter-argument p3 at first. But after c3 is provided, p can attack c2 by pointing out the contradiction with c3. This phenomenon cannot be formalized in argumentation system based on complete information about arguments and so we need a new framework.

Pioneer work this direction would far on be. asas APKC(Argumentation Procedure with Knowledge we know. Change)[Okuno08,Okuno09,Okuno10,Takahashi11] where counter-arguments, which cannot be used at the starting point of argumentation since these counter-arguments are not convinced by the agent itself, are triggered by other agents' arguments. In this paper, we extend this direction to provide more general framework than APKC. The difference between their works and this work are as follows:

- We let an agent give as many counter-arguments against other agent's arguments as they like where as APKC allows only one counter-argument against one argument at one turn.
- We do not employ any specific strategy how to make counter-argument whereas APKC imposes an agent to stick to one line of arguments until no counter-argument is made, then the agent change counter-argument in the other line of arguments.

To formalize the above, we introduce *sources of arguments* which represent usable arguments. This means that even if there are potential counter-arguments against the other agent's arguments, the agent cannot use the argument if the argument is not in the source. We also introduce *derivation rule of sources* which represent dynamic addition of arguments which were not initially able to be used, but later become usable based on the other agent's new arguments and its own belief. By these mechanisms, we let agents not know whether potential arguments would be usable in the future since there are incomplete information about the other agents' behavior.

Then, we show a computational method to decide which arguments are accepted by translating argumentation framework into logic programming from the God's viewpoint under the assumption that all possible arguments will always be presented by both parties sooner or later.

## 2 Framework for Argumentation under Incomplete Information

**Definition 1.** Let  $Arg_P(Arg_C, respectively)$  be a set called an argument set for  $P(C, respectively)^4$ . We write  $\langle Arg_P, Arg_C \rangle$  as Arg.

An attack relation for P(C, respectively),  $Attack_P(Attack_C)$  is a subset of

 $<sup>^4~</sup>P$  denotes "Pros" and "C" denotes "Cons".

 $Arg_P \times Arg_C(Arg_C \times Arg_P, respectively)$ . We write  $\langle Attack_P, Attack_C \rangle$  as Attack.

We say P(C, respectively) attacks n' by n if  $\langle n, n' \rangle \in Attack_P(Attack_C, respectively)$ .

Source<sub>P</sub> (Source<sub>C</sub>, respectively) is a subset of  $Arg_P$  ( $Arg_C$ , respectively). We write (Source<sub>P</sub>, Source<sub>C</sub>) as Source.

A set of derivation rules for P(C, respectively) Derive<sub>P</sub> (Derive<sub>C</sub>, respectively) is a set of the following rules of the form:

 $n \Leftarrow n_1, \dots n_m$ 

where  $n \in Arg_P$  ( $Arg_C$ , respectively) and  $n_i \in (Arg_P \cup Arg_C)(1 \le i \le m)$ . We call n the conclusion of the rule and  $n_i$ 's conditions of the rule. We write  $\langle Deriv_P, Derive_C \rangle$  as Derive

We call  $\langle Arg, Attack, Source, Derive \rangle$  an argumentation framework.

We assume that there is no loop in  $Attack_P \cup Attack_C$  to avoid infinite loop of arguments<sup>5</sup>.

In the above definition, a derivation rule enables an agent to augment its own source of arguments by adding the conclusion of the derivation rule if condition part is satisfied.

We define an argumentation tree which gives a semantics of acceptance of arguments as follows.

**Definition 2.** An argumentation tree  $Tr = \langle N, E \rangle$  w.r.t. an argumentation framework  $\langle Arg, Attack, Source, Derive \rangle$  is an in-tree<sup>6</sup> such that  $N \subset Arg_P \cup Arg_C$  and  $E \subset Attack_P \cup Attack_C$  and satisfies the following conditions:

- The root of Tr is  $p \in Source_P$  called "conclusion".
- If  $\langle n, n' \rangle \in E$  then either of the following holds.
  - $n \in Source_P$  and  $n' \in Source_C$  and  $\langle n, n' \rangle \in Attack_P$ .
  - $n \in Source_C$  and  $n' \in Source_P$  and  $\langle n, n' \rangle \in Attack_C$ .

Let  $Tr = \langle N, E \rangle$  be an argumentation tree.  $n \in N$  is accepted w.r.t. Tr if

- there is no edge to n, or
- there is no n' s.t.  $\langle n', n \rangle \in E$  and n' is accepted w.r.t. Tr.

Now, we can define a game called an *argumentation game* which gives a dialog between two parties. In argumentation game, agents can refer to source of arguments to produce counter-arguments.

**Definition 3.** A move of an argumentation game w.r.t. argumentation tree  $Tr = \langle N, E \rangle$  and a pair of source sets  $\langle S_P, S_C \rangle$  is an expansion of Tr,  $S_P$  and  $S_C$  defined as follows.

<sup>&</sup>lt;sup>5</sup> We may formalize an argumentation with loop if we follow Dung's stable extension or preferred extension. It is a future research topic.

<sup>&</sup>lt;sup>6</sup> An in-tree is an directed tree in which a single node is reachable from every other one (See Fig.1).

- -P's move is a set  $Move_P \subseteq Attack_P$  such that for every n such that  $\langle n, n' \rangle \in$  $Move_P, n \notin N, n \in Source_P$  and  $n' \in N$ . Then, a new set of nodes in a new argumentation tree N', a new set of edges in a new argumentation tree E' and a new pair of source sets  $\langle S'_P, S'_C \rangle$  becomes the following.
  - $N' = N \cup \{n | \langle n, n' \rangle \in Move_P\}$
  - $E' = E \cup Move_P$

  - $S'_P = S_P$   $S'_C = S_C \cup \{n | (n \Leftarrow n_1, ..., n_m) \in Derive_C \text{ and } n_i \in N'(1 \le i \le m) \}$
- -C's move is a set  $Move_C \subseteq Attack_C$  such that for every n such that  $\langle n, n' \rangle \in$  $Move_C, n \notin N, n \in Source_C$  and  $n' \in N$ . Then, a new set of nodes in a new argumentation tree N', a new set of edges in a new argumentation tree E' and a new pair of source sets  $\langle S'_P, S'_C \rangle$  becomes the following.
  - $N' = N \cup \{n | \langle n, n' \rangle \in Move_C\}$
  - $E' = E \cup Move_C$
  - $S'_P = S_P \cup \{n | (n \Leftarrow n_1, ..., n_m) \in Derive_P \text{ and } n_i \in N'(1 \le i \le m) \}$   $S'_C = S_C$

If both agents give  $\emptyset$  in consecutive two moves, then we say that the game is finished and we call a final tree after a game is finished argumentation game tree. Let Tr be an argumentation game tree  $\langle N, E \rangle$ . We say that a node  $n \in N$ is accepted w.r.t. the argumentation game tree Tr if n is accepted w.r.t. argumentation tree Tr.

Note that a move can be  $\emptyset^7$ , and a conclusion is decided to be accepted or not using the argumentation game tree.

Example 1. Consider the example discussed at Introduction. Then,

 $Arg_P = \{p0, p1, p2, p3\}$  $Arg_C = \{c1, c2, c3\}$  $Attack_P = \{ \langle p1, c1 \rangle, \langle p2, c1 \rangle, \langle p3, c2 \rangle \},\$  $Source_P = \{p0, p1, p2\},\$  $Derive_P = \emptyset$  $Attack_C = \{ \langle c1, p0 \rangle, \langle c2, p1 \rangle, \langle c3, p2 \rangle \},\$  $Source_C = \{c1, c2, c3\},\$  $Derive_C = \{c3 \leftarrow p3\}$ 

Note that since initial  $Source_P$  does not include p3 so we cannot use an attack to c2 by p3.

- 1. Let p0 be a conclusion. Then  $Tr = \langle \{p0\}, \emptyset \rangle.$
- 2. C's next move has two possibilities, that is, to give either  $\emptyset$  or  $\{\langle c1, p0 \rangle\}$ .
- 3. Suppose that C gives  $\{\langle c1, p0 \rangle\}$ Then,  $Tr = \langle \{p0, c1\}, \{\langle c1, p0 \rangle \} \rangle$ .
- 4. P's next move has four possibilities, that is, to give either  $\emptyset$  or  $\{\langle p1, c1 \rangle\}$  or  $\{\langle p2, c1 \rangle\}$  or  $\{\langle p1, c1 \rangle, \langle p2, c1 \rangle\}.$

<sup>&</sup>lt;sup>7</sup> This means that even if there are possible counter-arguments, an agent can be silent.

5. Suppose that P gives  $\{\langle p1, c1 \rangle, \langle p2, c1 \rangle\}$ . Then,

 $Tr = \langle \{p0, c1, p1, p2\}, \{\langle c1, p0 \rangle, \langle p1, c1 \rangle, \langle p2, c1 \rangle \} \rangle.$ 

- 6. C's next move has four possibilities, that is, to give either  $\emptyset$  or  $\{\langle c2, p1 \rangle\}$  or  $\{\langle c3, p2 \rangle\}$  or  $\{\langle c2, p1 \rangle, \langle c3, p2 \rangle\}$ .
- 7. Suppose that C gives  $\{\langle c2, p1 \rangle, \langle c3, p2 \rangle\}$ . Then,  $Tr = \langle \{p0, c1, p1, p2, c2, c3\}, \{\langle c1, p0 \rangle, \langle p1, c1 \rangle, \langle p2, c1 \rangle, \langle c2, p1 \rangle, \langle c3, p2 \rangle\} \rangle$ . Then, since  $(c3 \Leftarrow p3) \in Derive_C$ ,  $Source_P$  becomes  $\{p0, p1, p2, p3\}$ .
- 8. P's next move has only two possibilities, that is, to give  $\{\langle p3, c2 \rangle\}$  or  $\emptyset$  since p3 is now in  $Source_P = \{p0, p1, p2, p3\}$  and  $\langle p3, c2 \rangle$  becomes usable.
- 9. Suppose that P gives  $\{\langle p3, c2 \rangle\}$ . Then,
  - $Tr = \langle \{p0, c1, p1, p2, c2, c3, p3\},$
  - $\{\langle c1, p0 \rangle, \langle p1, c1 \rangle, \langle p2, c1 \rangle, \langle c2, p1 \rangle, \langle c3, p2 \rangle, \langle p3, c2 \rangle\} \rangle.$
- 10. There is no move from both sides so the game is finished.
- 11. Then, p3 is accepted and so c2 is not accepted. Then p1 is accepted and c1 is not accepted. Finally p0 is accepted.

In this example, p3 is a key to rebut c2 and p3 was not in initial source but is invoked after c3 is made. This invocation is made by a derivation rule  $p3 \leftarrow c3$  (See Fig.1).



Fig. 1. Representation of Arguments and Derive Relation for Example 1

There are many ways to develop an argumentation game tree, but we can show that a final argumentation tree will be unique in any way of developing a tree if both parties eventually give all possible arguments. We call this strategy *eager*, so we can say that an argumentation game tree will converge into one if both agents are eager. On the other hand, we can define a *lazy* agent which gives only necessary counter-arguments. In other words, a lazy agent will choose one counter-argument among possible counter-argument against the other agent's argument and it will choose another counter-argument only if the chosen counterargument is rebutted by the other agent's counter-counter-argument. Then, in this lazy agent's case some of derivation rules might not be invoked so that an effective counter-argument might not be produced. We show such an example as follows.

*Example 2.* Consider the following case where we add  $\langle c4, p2 \rangle$  to  $Attack_C$  of the previous example. Then,

$$\begin{split} Attack_P &= \{ \langle p1, c1 \rangle, \langle p2, c1 \rangle, \langle p3, c2 \rangle \},\\ Source_P &= \{ p0, p1, p2 \},\\ Derive_P &= \emptyset\\ Attack_C &= \{ \langle c1, p0 \rangle, \langle c2, p1 \rangle, \langle c3, p2 \rangle, \langle c4, p2 \rangle \},\\ Source_C &= \{ c1, c2, c3, c4 \},\\ Derive_C &= \{ c3 \leftarrow p3 \} \end{split}$$

We show an example when an agent does not give full arguments but hides an argument.

- 1. Let p0 be a conclusion. Then  $Tr = \langle \{p0\}, \emptyset \rangle.$
- 2. C's next move has two possibilities, that is, to give either  $\emptyset$  or  $\{\langle c1, p0 \rangle\}$ .
- 3. Suppose that C gives  $\{\langle c1, p0 \rangle\}$ Then,  $Tr = \langle \{p0, c1\}, \{\langle c1, p0 \rangle\} \rangle$ .
- 4. P's next move has four possibilities, that is, to give either  $\emptyset$  or  $\{\langle p1, c1 \rangle\}$  or  $\{\langle p2, c1 \rangle\}$  or  $\{\langle p1, c1 \rangle, \langle p2, c1 \rangle\}$ .
- 5. Suppose that P gives  $\{\langle p1, c1 \rangle, \langle p2, c1 \rangle\}$ . Then,
- $Tr = \langle \{p0, c1, p1, p2\}, \{\langle c1, p0 \rangle, \langle p1, c1 \rangle, \langle p2, c1 \rangle \} \rangle.$
- 6. C's next move has eight possibilities, that is, to give a subset of  $\{\langle c2, p1 \rangle, \langle c3, p2 \rangle, \langle c4, p2 \rangle\}$ .
- 7. Suppose that C gives  $\{\langle c2, p1 \rangle, \langle c4, p2 \rangle\}$ . Then,

 $Tr = \{ \{ p0, c1, p1, p2, c2, c4 \},\$ 

 $\{\langle c1, p0 \rangle, \langle p1, c1 \rangle, \langle p2, c1 \rangle, \langle c2, p1 \rangle, \langle c4, p2 \rangle\} \}.$ 

Note that since C did not choose  $\langle c3, p2 \rangle$ , we cannot make p3 usable.

- 8. Only *P*'s next move is to give  $\emptyset$ .
- 9. C hides the another counter-argument  $\{c3, p2\}$  and gives  $\emptyset$ . Then, there is no move from both sides so we are done.
- 10. Then, c2 and c4 are accepted. Then either p1 nor p2 is accepted and c1 is accepted. Finally p0 is not accepted.

In this example, an agent c does not use c3 to rebut p2 but use c4 therefore, p3 is not invoked and p0 is not accepted. An agent c does not need to make more argument using c3 since the current counter-arguments are enough to win the example (See Fig. 2).



Fig. 2. Representation of Arguments for Example 2

#### **3** Computing Acceptance in Argumentation Framework

In this section, we assume that agents are both eager. Then we can translate an argumentation framework into a logic program in order to compute acceptability of a given argument from the bird's eye view. There is a proposal of computing Dung's argumentation semantics by translating the Dung's framework into a logic program and corresponding answer set of the program with acceptability[Osorio05]. We extend their work by adding an extra condition reasoning about "sources". In order to do so, we introduce new predicate "announced(A)" meaning that an argument A is actually used for building an argumentation game tree. If an argument can be attacked by satisfying the condition that there is an attack relation for the argument and counter-argument is in the source, then counter-argument becomes *announced* to the other agent so that the agent can use other sources of arguments.

**Definition 4.** Let  $\langle Arg, Attack, Source, Derive \rangle$  be an argumentation framework. For  $A \in Arg_P \cup Arg_C$ , we define  $Counter_A = \{B | \langle B, A \rangle \in Attack_P \cup Attack_C\}$ . For each argument A, we define the translation of argument A to rules of logic programming as follows:

$$accepted(A) \leftarrow \bigwedge_{B \in Counter_A} not \ (source(B) \land accepted(B)).$$

Note that if  $Counter_A$  is empty then the above rule becomes accepted(A). For every  $B \in Counter_A^8$ ,

 $announced(B) \leftarrow announced(A) \land source(B).$ 

<sup>&</sup>lt;sup>8</sup> If the parent node is announced and the current node is in the source, then the current node will be announced. This rule expresses the eager strategy of argumentation.

We also add the following rules for  $(A \Leftarrow A_1, ..., A_m) \in Derive_C$ :

$$source(A) \leftarrow \bigwedge_{i=1}^{m} body_C(A_i).$$

where  $body_C(A_i)$  is defined as follows:

$$body_C(A_i) = \begin{cases} source(A_i) & \text{if } A_i \in Arg_C \\ announced(A_i) & \text{if } A_i \in Arg_P \end{cases}$$

Similarly, we add the following rules for  $(A \leftarrow A_1, ..., A_m) \in Derive_P$ :

$$source(A) \leftarrow \bigwedge_{i=1}^{m} body_P(A_i)$$

where  $body_P(A_i)$  is defined as follows:

$$body_P(A_i) = \begin{cases} source(A_i) & \text{if } A_i \in Arg_P\\ announced(A_i) & \text{if } A_i \in Arg_Q \end{cases}$$

We also add the following for an argument A in the initials source sets:

source(A).

We also add the following for the conclusion  $A_0$  which is the root of the argumentation game tree:

announced $(A_0)$ .

Note that since there is no loop in the attack set, the above program becomes a stratified program so there is a unique minimum model for the translated program.

*Example 3.* Consider the setting of Example 1. The translated logic program becomes as follows:

```
announced(c3) \leftarrow announced(p2) \land source(c3).
source(p3) \leftarrow announced(c3).
source(p0). source(p1). source(p2).
source(c1). source(c2). source(c3).
announced(p0).
```

Then, we can show that accepted(p0) is derived from the above program.

**Theorem 1.** Let  $\langle Arg, Attack, Source, Derive \rangle$  be an argumentation framework and  $A_0$  be a conclusion and Tr be a final argumentation game tree w.r.t. the framework for the eager strategy and Pr be a translated logic program from the framework. Then,  $A_0$  is accepted if and only if  $Pr \models accepted(A_0)$ 

### 4 Related Works

Several studies have been conducted on argumentation semantics. Dung provided a semantics for a given abstract argumentation framework based on acceptability [Dung95]. He defined several acceptable sets, depending on the range of strength against an attack. Coste-Morquis et al. argued that it is controversial to include both agents' arguments in an extension because this would indicate an indirect attack [Coste-Marquis05]. They defined a new semantics, called "prudent semantics," which does not allow such controversial cases, and compared this with Dung's semantics. Other semantics have also been proposed, such as ideal semantics [Dung06], semi-stable semantics from the viewpoint of skepticism [Baroni07]. All these semantics involved argumentation systems from a static viewpoint, whereas our proposed semantics is suitable for a dynamic argumentation system.

Cayrol et al. studied how acceptable arguments are changed when a new argument is added to Dung's argumentation system *before an argumentation is executed* [Cayrol08,Cayrol10]. Therefore, it is along the line of usual belief revision approach where revision is made before reasoning and revision never occurs during reasoning. In contrast, we focus on addition or arguments during argumentation. So, we believe our approach has more dynamic nature.

García et al. formalized argumentation based on Defeasible Logic Programming (DeLP) [Garcia07]. In DeLP, agent's knowledge base consists of two kinds of rules: strict rules and defeasible rules. The result of argumentation is different depending on which defeasible rules are used. Afterwards, Moguillansky discussed revision of the knowledge base [Moguillansky08]. In his method, after constructing the initial argumentation tree called dialectical tree, knowledge base is changed by extracting defeasible rules and the tree is altered. The goal is to construct undefeated argumentation by selecting suitable defeasible rules. They presented an algorithm for this alteration of the tree and considered a strategy to get the undefeated argumentation. In a series of studies, they formalized several properties in argumentation based on this approach [Lucer009]. Again the revision of knowledge base in their work is made before an argumentation is executed. Cobo et al. proposed an argumentation framework in which available arguments change depending on time intervals [Cobo10]. In their work, these intervals are given in advance, they did not consider the mechanism by which an argument causes to generate a new argument. In contrast, we focus specifically on the effect of knowledge gained from presented arguments, which is essential in actual argumentation.

Prakken formalized an argument game and showed that counter-argument might not be effective in a game if it is added dynamically and proposed a notion of relevance to make counter-argument effective[Prakken01]. However, in this work, possible arguments are already defined before the game and are never added whereas in our work possible arguments are added according to other party's argument.

Argumentation-based approach is applied to formalize processes appeared in agents communication such as negotiation[Amgoud00]. Considering the effect of the execution of arguments, agents communication are rather related issue, since belief of each agent is updated on receiving information from the other agent. Amgoud proposed the protocol that handles arguments and formalized the case in accepting/rejecting new information [Amgoud00]. She also presented a general framework for argumentation-based negotiation in which agent has a theory and it evolves during a dialogue [Amgoud08]. She considered the knowledge base for each agent separately, as well as its revision by exchanging arguments. The significant difference between her work and ours is that in her approach, an attack relation is increased only between a previous argument and the currently proposed argument whereas in our approach, a dynamic addition of an attack relation does not have such restriction so that we can add any attack relation using *Derive* and *Source*.

#### 5 Conclusion

The contributions of the paper are as follows.

- We give more general framework of argumentation under incomplete information.
- We give a computational method of how to decide the acceptability of the arguments using a translation from an argumentation framework to a logic program under the assumption that every possible arguments are made.

As a future research, we would like to pursue the following.

- We should give a computational method of acceptability for a lazy agent. The method must reflect multiple extensions of arguments related with choices of arguments.
- We would like to introduce the strength of arguments which is related with legal significance.
- We would like to consider how we could apply this framework to reason about a response which could make "a trap" against the opponent where some of opponent responses could cause contradiction in another line of arguments.

#### References

- Amgoud00. Amgoud, L., Parsons, S., and Maudet, N., "Arguments, Dialogue, and Negotiation", Proc. of ECAI2000, pp.338 342 (2000).
- Amgoud08. Amgoud, L., Dimopolos, Y., and Moraitis, P., "A General Framework for Argumentation-Based Negotiation", Proc. of ArgMAS2007, LNCS 4946, pp.1 – 17 (2008).
- Baroni07. Baroni P., and Giacomin, M., "Comparing Argumentation Semantics with Respect to Skepticism", Symbolic and Quantitative Approaches to Reasoning with Uncertainty, pp. 210 – 221, LNCS 4724 (2007).
- Cayrol08. Cayrol, C., D.de St-Cyr, F., and Lagasquie-Shiex, M-C, "Revision of an argumentation system". Proc. of KR2008, pp. 124 134 (2008).
- Cayrol10. Cayrol, C., D.de St-Cyr, F., and Lagasquie-Shiex, M-C, "Change in Abstract Argumentation Frameworks: Adding an Argument", Journal of Artificial Intelligence Research, Vol. 38, pp. 49 – 84 (2010).
- Caminada06. Caminada, M., "Semi-stable Semantics", Proc. of COMMA2006, pp. 121 130 (2006).
- Cobo10. Cobo, M.L., Martinez D.C., and Simari, G.R., "An Approach to Timed Abstract Argumentation", Proc. of NMR2010, Workshop on Argument, Dialog and Decision (2010).
- Coste-Marquis05. Coste-Marquis, S., Devred C., and Marquis, P., "Prudent Semantics for Argumentation Frameworks", Proc. of ICTAI2005, pp.568 – 572 (2005).
- Dung95. Dung, P. M., "On the Acceptability of Arguments and its Fundamental Role in Nonmonotonic Reasoning, Logic Programming and N-Person Games", Artificial Intelligence, Vol. 77, pp.321 – 357 (1995).
- Dung06. Dung, P.M., Mancarella, P., and Toni, F., "A Dialectic Procedure for Sceptical, Assumption-based Argumentation", Proc. of COMMA2006, pp. 145 – 156 (2006).
- Garcia07. García, A., Chesnevar, C., Rotstein, N., and Simari, G., "An Abstract Presentation of Dialectical Explanations in Defeasible Argumentation", Proc. of ArgNMR07, pp. 17 – 32 (2007).
- Lucero<br/>09. Lucero, M.J.G., Chesñever C.I., and Simari, G.R., "On the Accrual of Arguments in Defeasible Logic Programming", Proc. of IJCAI2009, pp. 804 809 (2009).
- Modgil09. Modgil, S., "Reasoning about Preferences in Argumentation Frameworks", Artificial Intelligence, Vol. 173, pp.901-1040 (2009).
- Moguillansky08. Moguillansky, M.O., et al., "Argument Theory Change Applied to Defeasible Logic Programming", Proc. of AAAI2008, pp. 132 – 137 (2008).
- Osorio05. Osorio, M., Zepeda, C, Nieves, J. C., Corte's, U., "Inferring Acceptable Arguments with Answer Set Programming", http://www.lsi.upc.edu/~jcnieves/JCNieves-Publications/Conference/ ENC05.pdf, Proc. of ENC'05, pp.198 205 (2005).
- Okuno 8. Okuno K., and Takahashi, K., "Argumentation with a Revision of Knowledge Base", Proc. of EUMAS08, CD-ROM, December (2008).
- Okuno<br/>09. Okuno, K., Takahashi, K., "Argumentation System with Changes of an<br/> Agent's Knowledge Base", Proc. of IJCAI 2009, pp.226–232 (2009).
- Okuno10. Okuno, K., Takahashi, K., "Argumentation System Allowing Suspend/Resume of an Argumentation Line", Proc. of ArgMAS2010, pp.145–162 (2010).

- Prakken<br/>01. Prakken, H., "Relating Protocols for Dynamic Dispute with Logics for<br/> Defeasible Argumentation", Synthese Vol. 127, pp. 187 219 (2001).
- Rahwan09. I.Rahwan, and G.Simari (eds.), "Argumentation in Artificial Intelligence", Springer (2009).
- Takahashi11. Takahashi, K., Nambu, Y., "A Semantics for Dynamic Argumentation Frameworks", Proc. of ArgMAS2011 (2011)